

# Dependable and Coordinated Resources Allocation Algorithms for Distributed Computing

[Victor Toporkov](#)



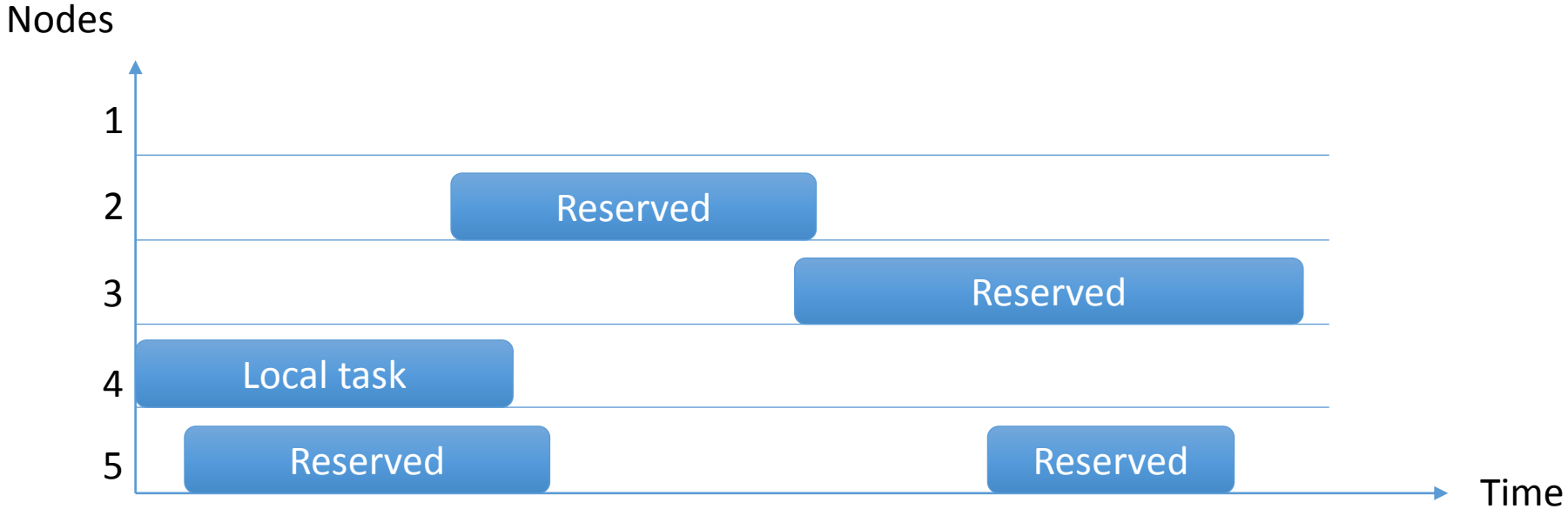
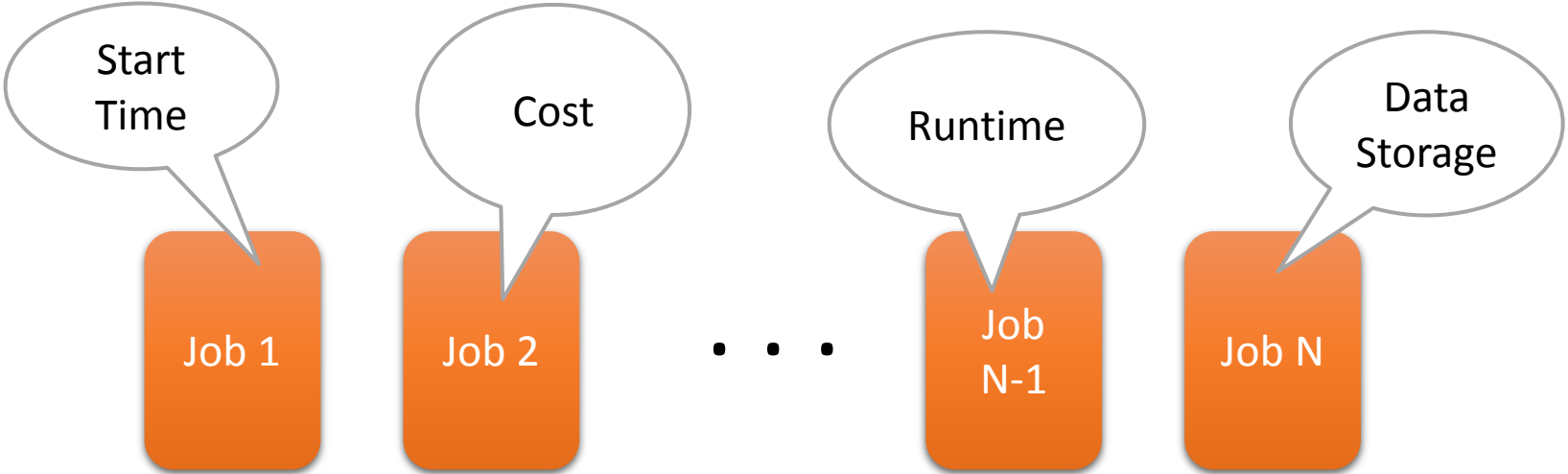
and Dmitry Yemelyanov

National Research University “Moscow Power Engineering Institute”

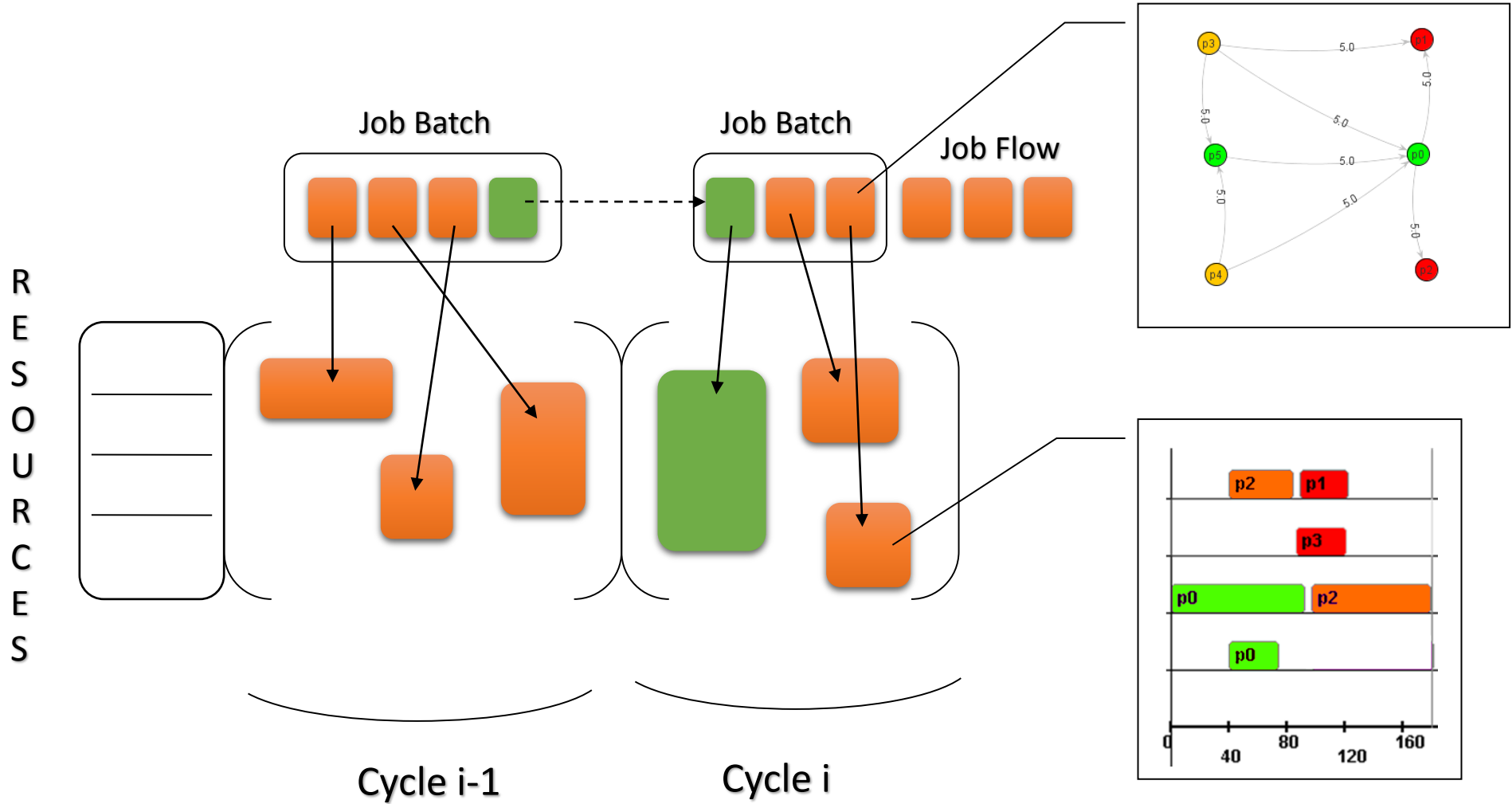
# Introduction

- **Resource co-allocation** and scheduling of complex sets of parallel jobs is an essential issue in distributed environments with non-dedicated resources
- **Economic models** are used to solve resource sharing and scheduling problems in a transparent and an efficient way in cloud computing, utility Grids, and multi-agent systems
- The main aspect of job-flow scheduling is its **efficiency** in terms of **QoS** and resources utilization

# Job Flow Scheduling Problem



# Job Flow Scheduling: *V. Toporkov et al. 2017. Cyclic Anticipation Scheduling in Grid VO's with Stakeholders Preferences. PaCT 2017, LNCS 10421, pp. 372–383.*



# Job Resource Request

The resource requirements are arranged into a resource request containing:

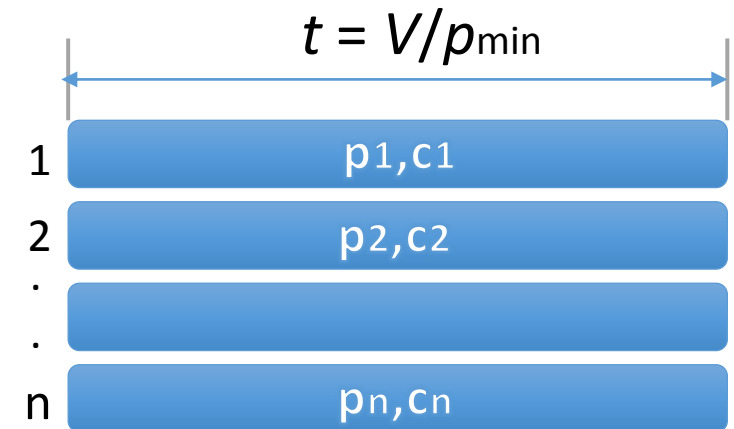
$n$  - number of simultaneously reserved computational nodes

$p$  - minimal performance requirement for each computational node

$V$  - computational volume for a single node task

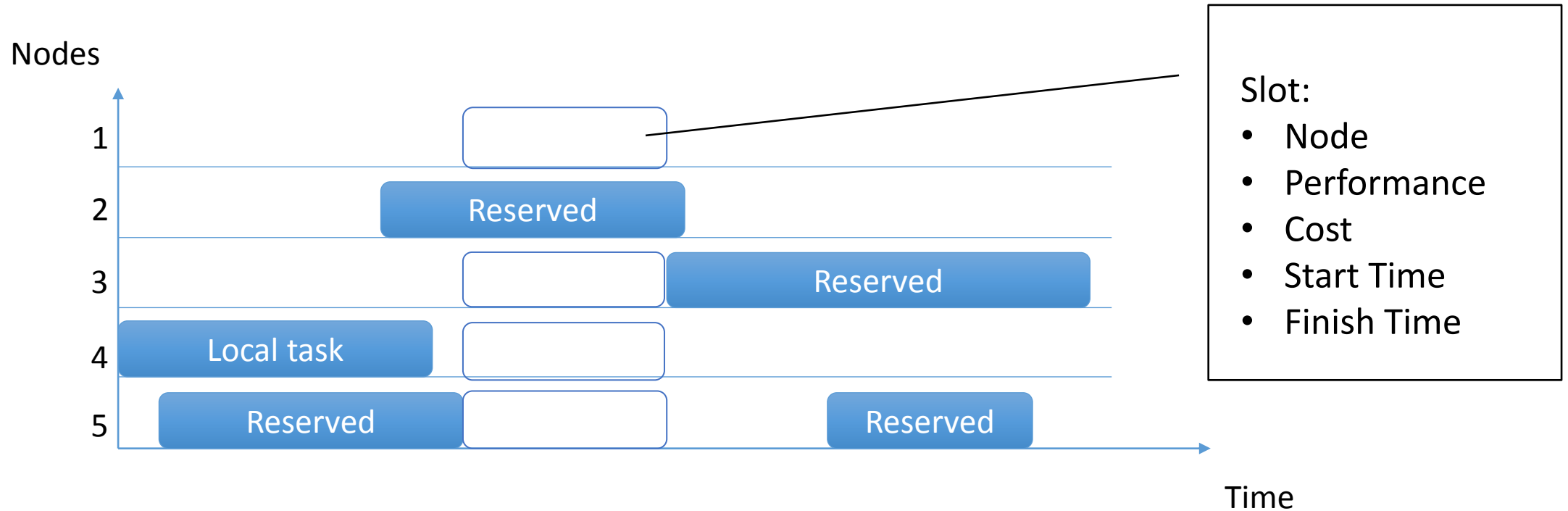
$C$  - maximum total job execution cost (budget)

$Z$  - preferred job optimization criterion



# Window Search Problem

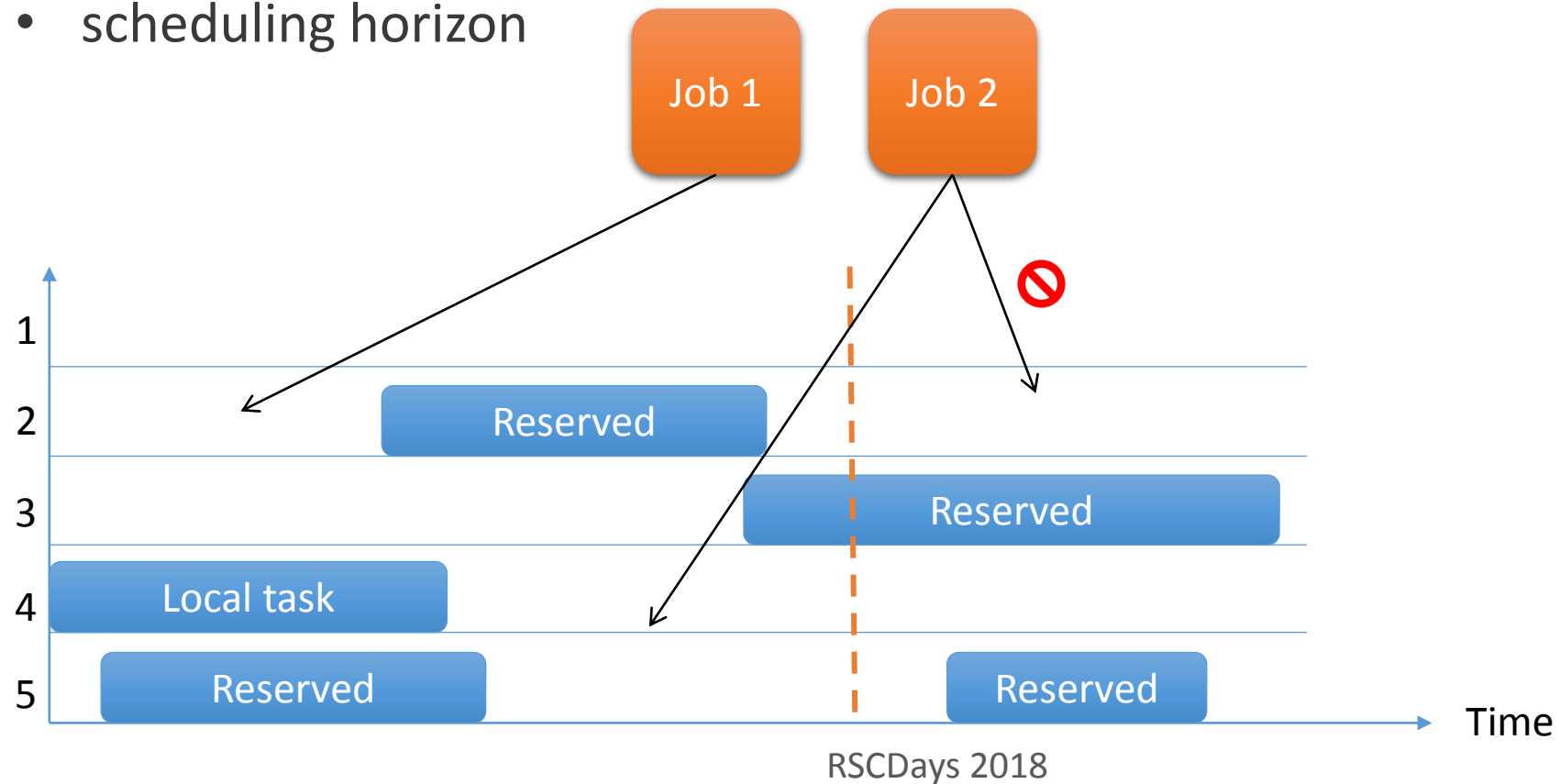
Allocate a window of **four** nodes for a time  $T$ , with requirements on nodes performance and total cost. Minimize window start time:



# Deadline and Scheduling Horizon

There's a practical limit on the slots availability:

- deadline
- backfilling
- scheduling horizon



# General Window Search Scheme

All available time-slots are **ordered by the start time**;

**for each**  $p_i$  in  $(p_{\min}; p_{\max})$  {

**while** there is at least one slot available {

- Add next available slot to the window list;
- Check all slots in the window considering required length  $t = V/p_{\min}$  and **remove** the slots being late;
- Select  **$n$ -slot** window best by the given user criterion  $Z$ ;

}

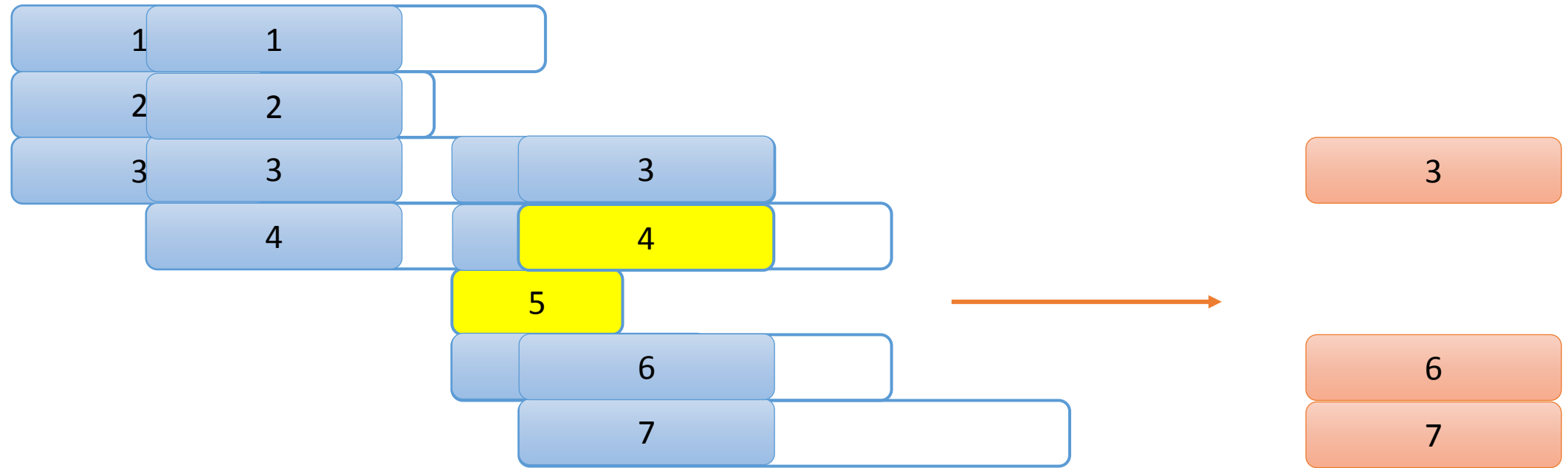
}

**return** the best of the found interim windows;

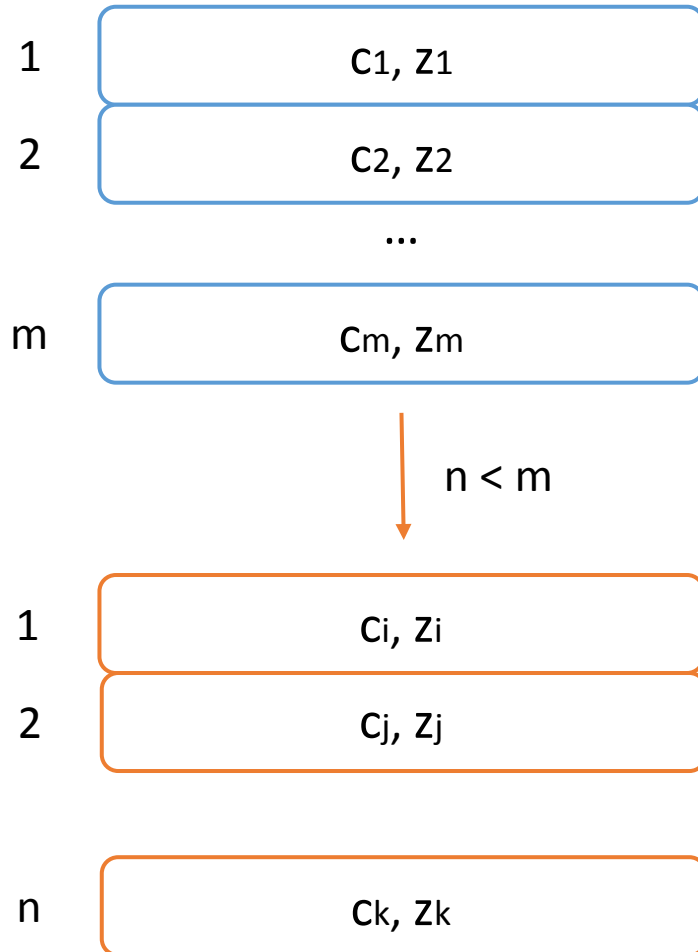


# Window Search Scheme Visualized

Slots



# Optimal Slots Subset Allocation



Maximize:

$$Z = x_1 z_1 + x_2 z_2 + \dots + x_m z_m,$$

$$x_1 c_1 + x_2 c_2 + \dots + x_m c_m \leq C$$

$$x_1 + x_2 + \dots + x_m = n$$

$$x_i \in \{0, 1\}, i = 1, \dots, m,$$

# Optimization Scheme

## 0-1 Knapsack Problem with $O(m * C)$

$$f_i(C_j, n_k) = \max\{f_{i-1}(C_j, n_k), f_{i-1}(C_j - c_i, n_k - 1) + z_i\},$$

$$i = 1, \dots, m, j = 1, \dots, C, k = 1, \dots, n,$$

i

→

Cj

↓

k=1	c=3 z=3	c=2 z=1	c=4 z=6
0	-	-	-
1	-	-	-
2	-	1	1
3	3	3	3
4	3	3	6
5	3	3	6
6	3	3	6

k=2	c=3 z=3	c=2 z=1	c=4 z=6
0	-	-	-
1	-	-	-
2	-	-	-
3	-	-	-
4	-	-	-
5	-	4	4
6	-	4	7

$$O(m * n * C)$$

$$n \ll m$$

$$n \ll C$$

# Simulation Study <https://github.com/dmieter/mimapr>

## Intel Core i3-4130, 16GB RAM

Simulation environment:

- heterogeneous resource domain model

$N = 100$  computing nodes

$L = 1200$  scheduling horizon

- non-linear probabilistic model for the computing environment parameters generation: cost, performance, initial load
- a space-shared resources allocation policy

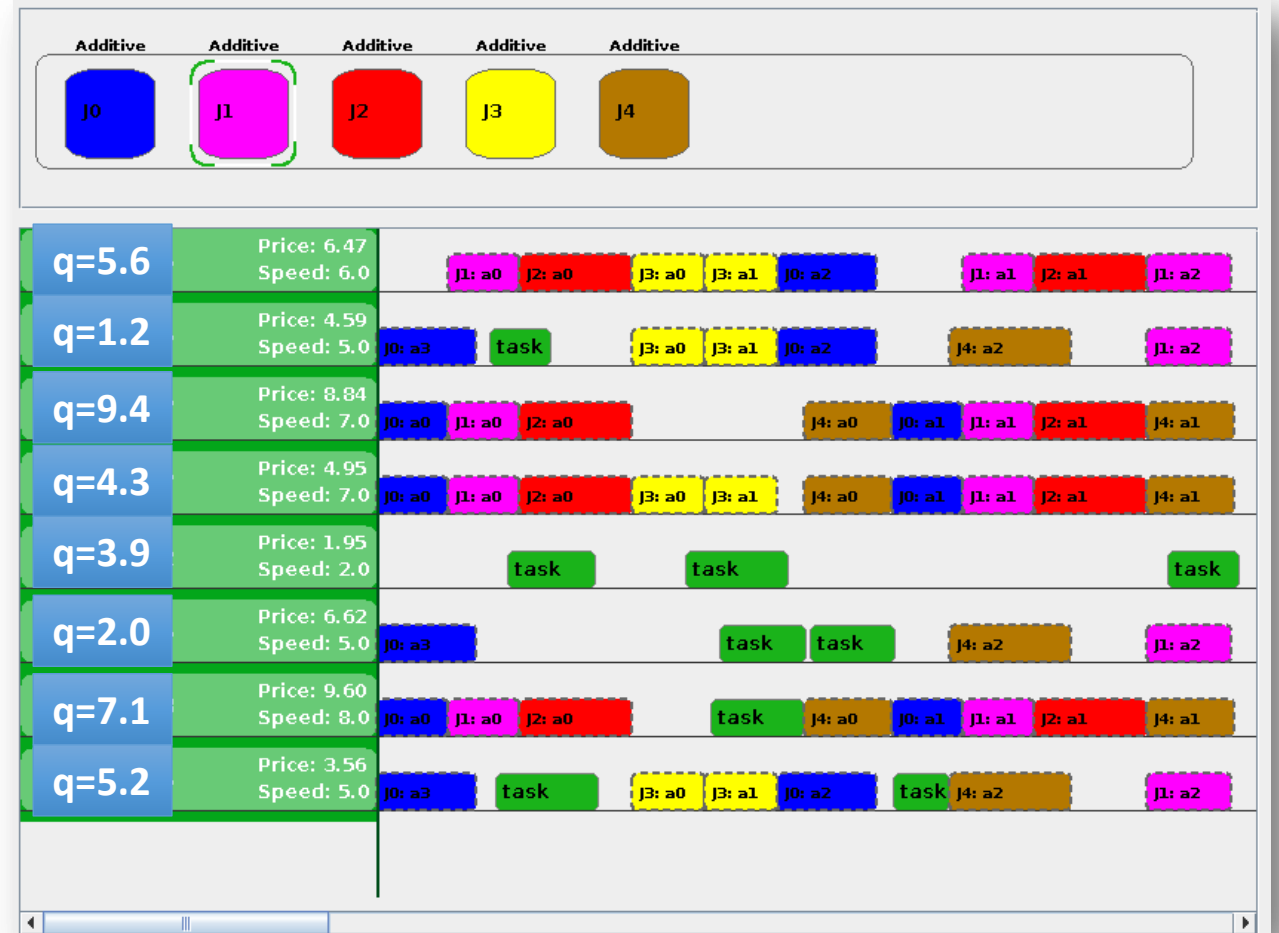
Job request:

$n = 7$  nodes

$V = 800$  computational volume

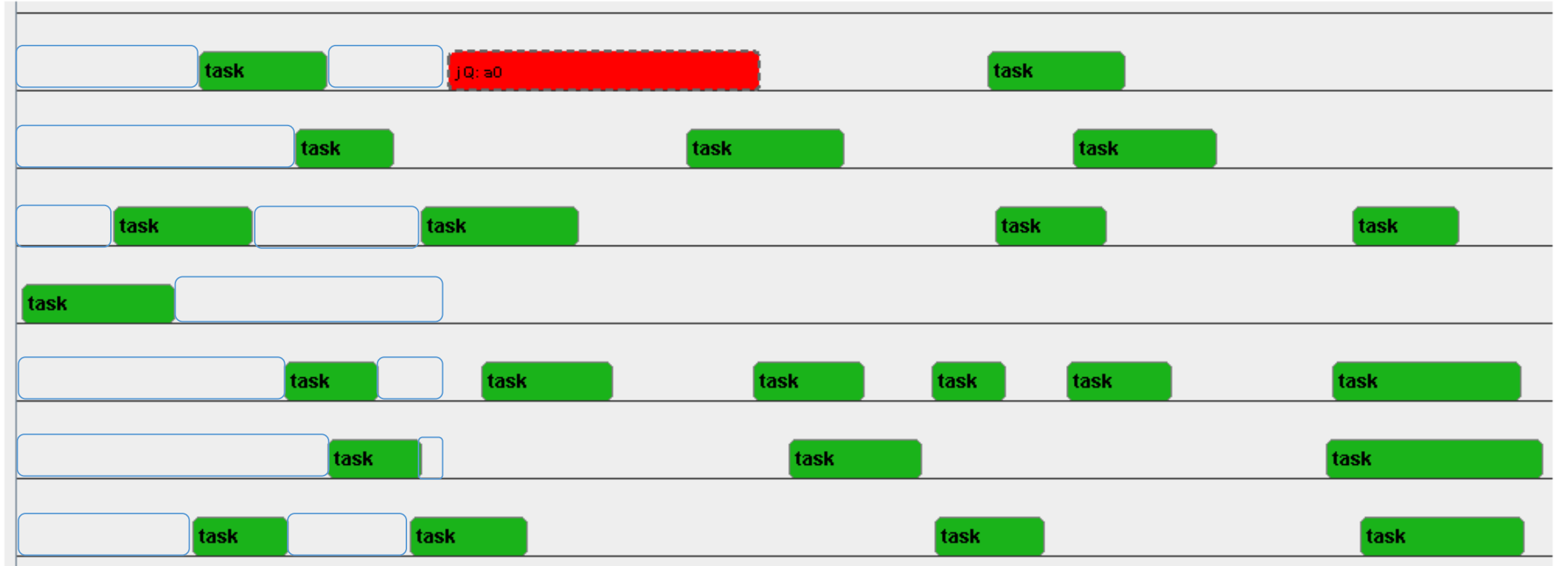
$C = 644$  maximum budget

$q_i$  in  $[0;10]$  randomly generated for each node to compare algorithms against  $Q$  (sum of  $q_i, i = 1, \dots, n$ )



# Resource Domain Utilization Example

Nodes



Time

# Algorithms Comparison

- **First Fit** returns first suitable and affordable window found
- **Multiple Best** returns the best window over a set of execution alternatives found
- **General Window Search Scheme:**
  - Min Finish Time
  - Min Runtime
  - Min Cost
- **Max Q** additionally implements an optimal slots subset allocation

Kovalenko et al., 2007  
Buyya et al., 2007

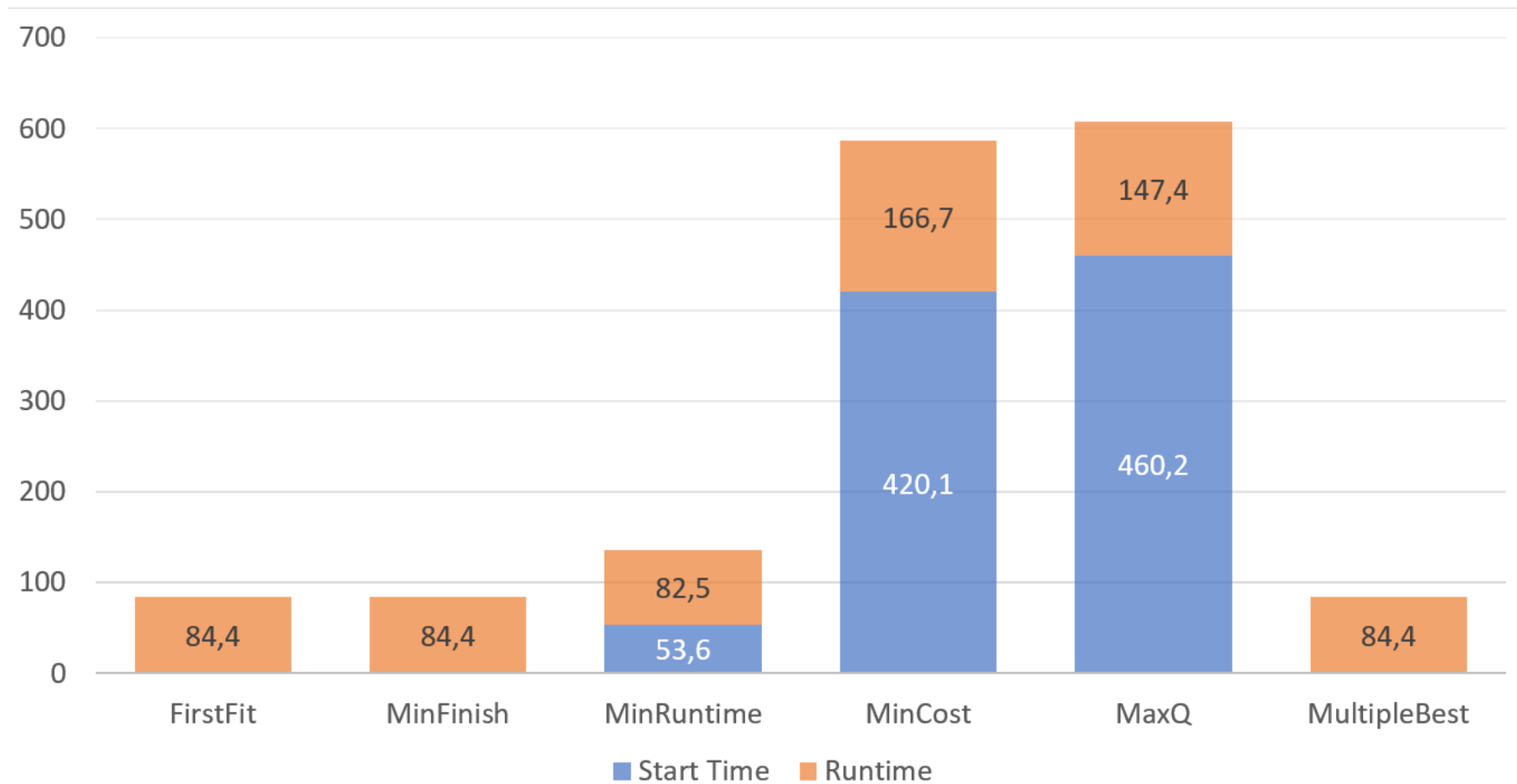
Ernemann et al., 2002



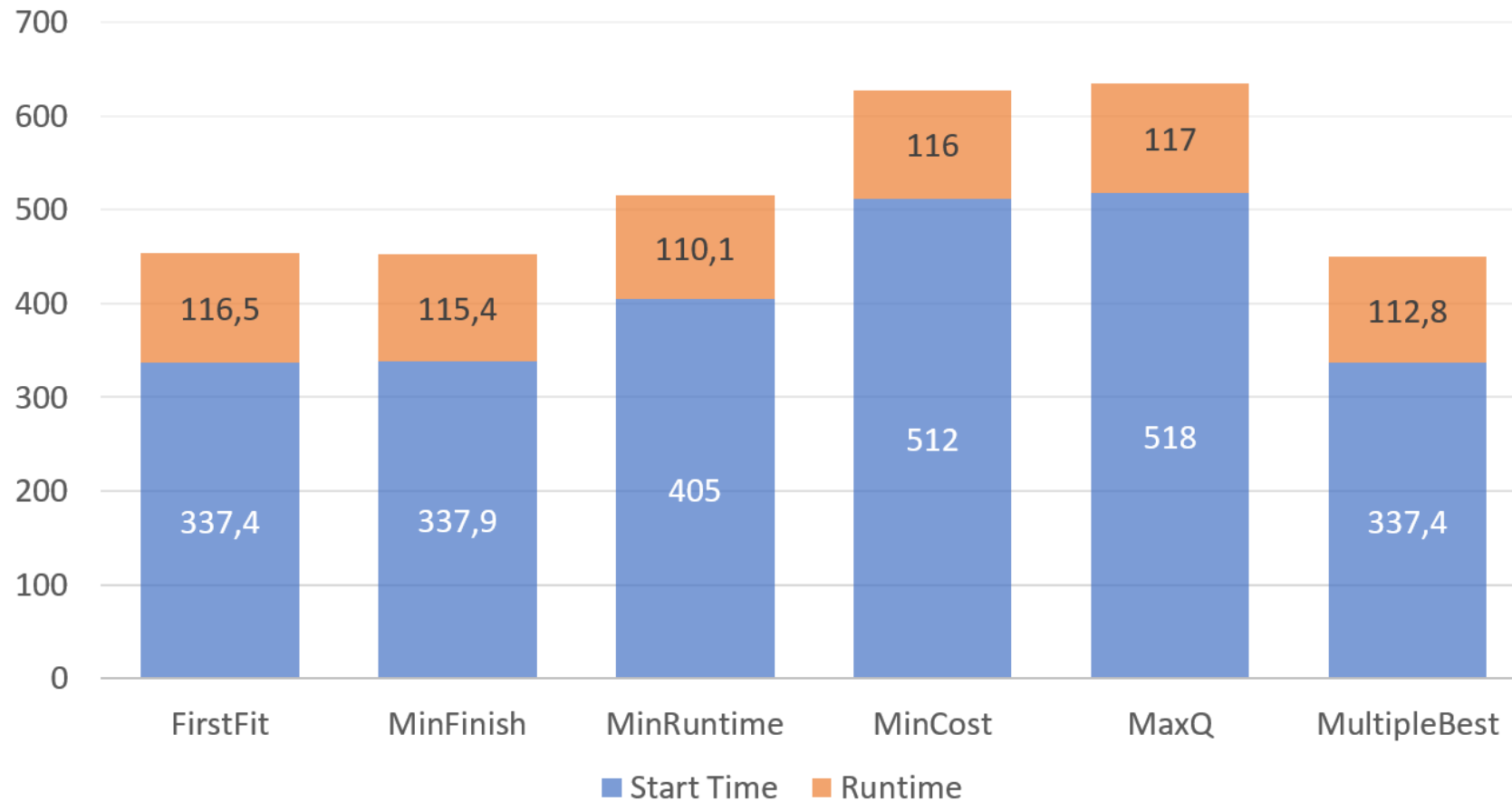
Toporkov et al., 2012

Toporkov,  
Yemelyanov, 2018

# Simulation Study: Time I (7 nodes out of 100)

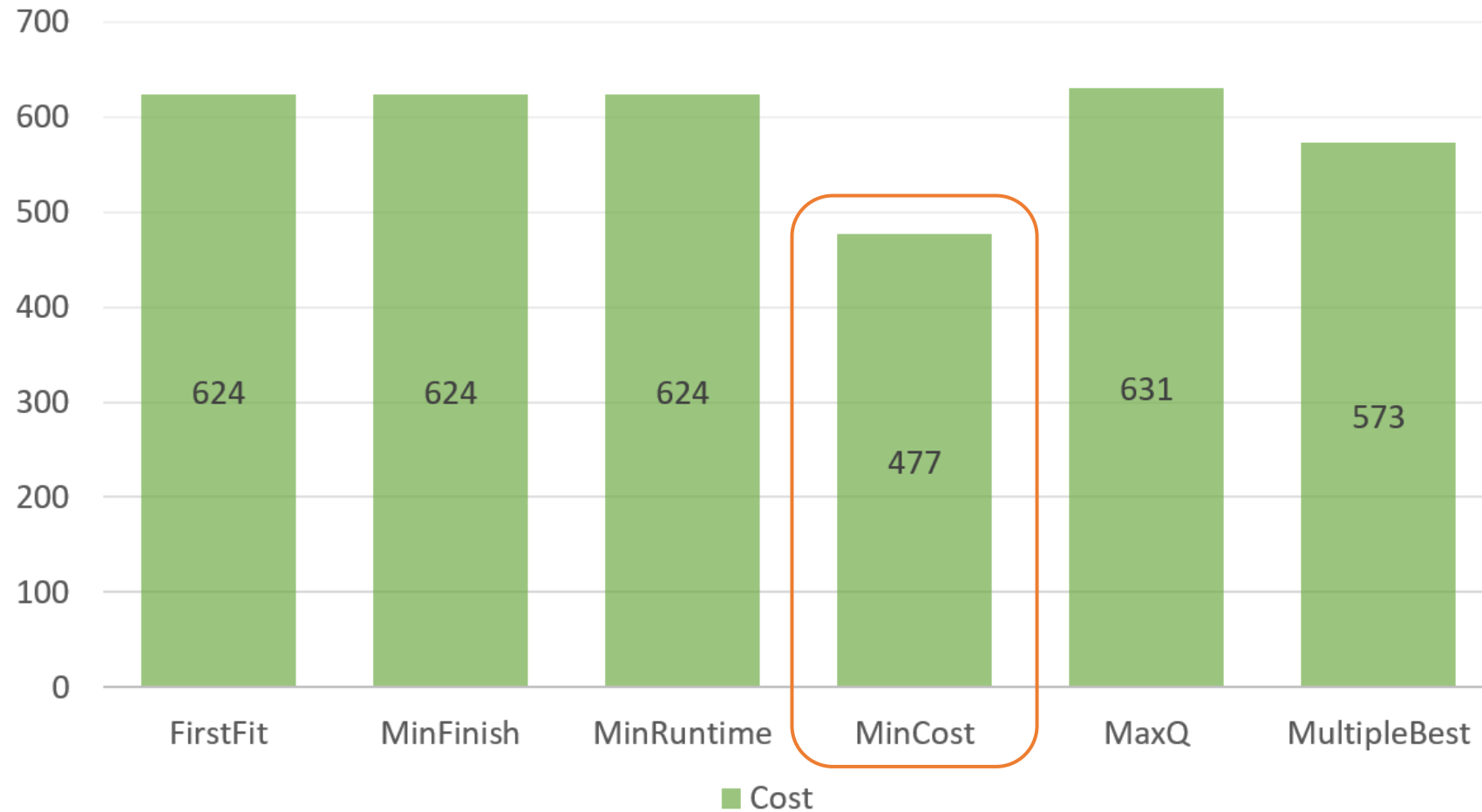


# Simulation Study: Time II (7 nodes out of 40)



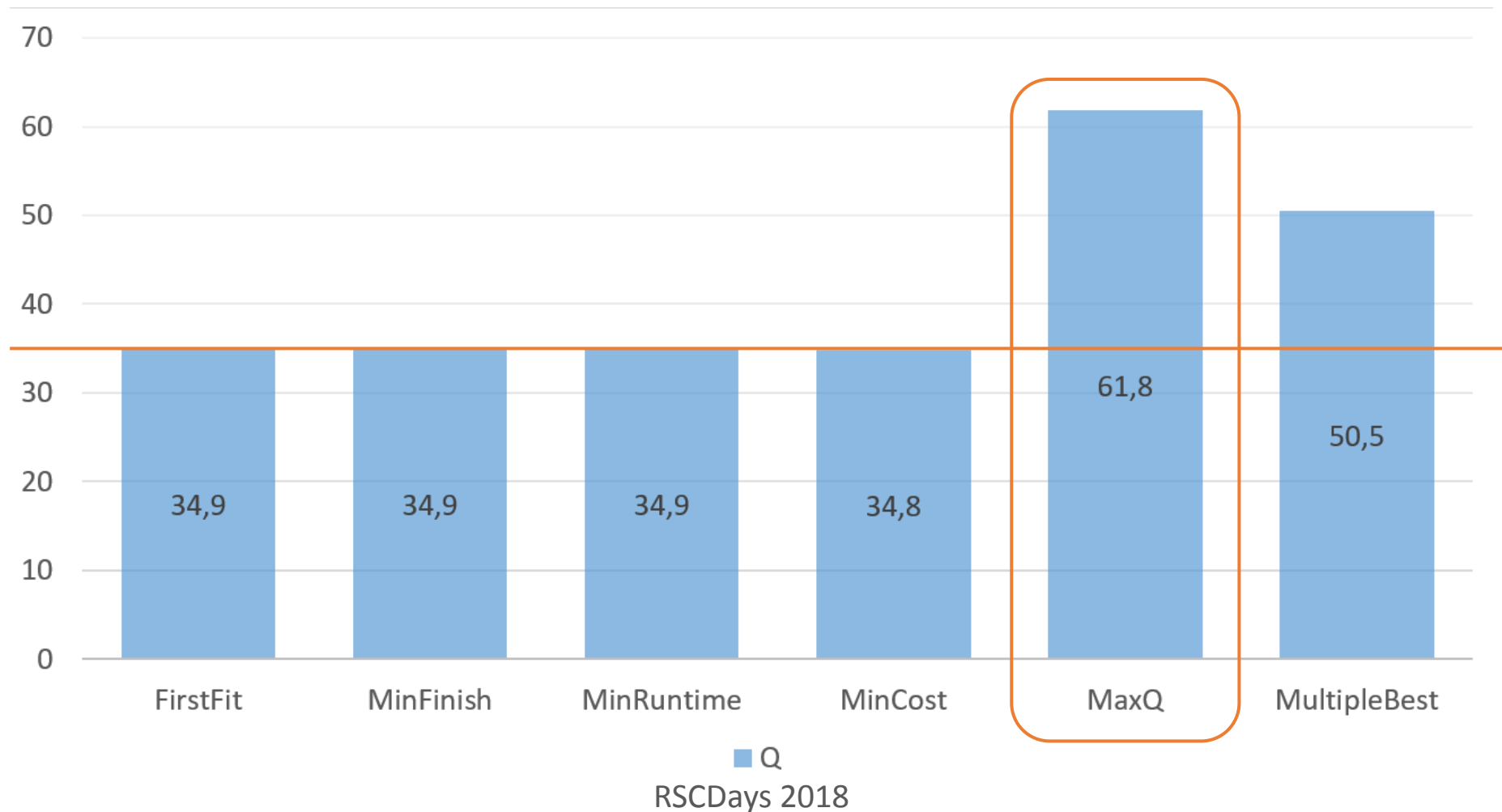


# Simulation Study: Execution Cost



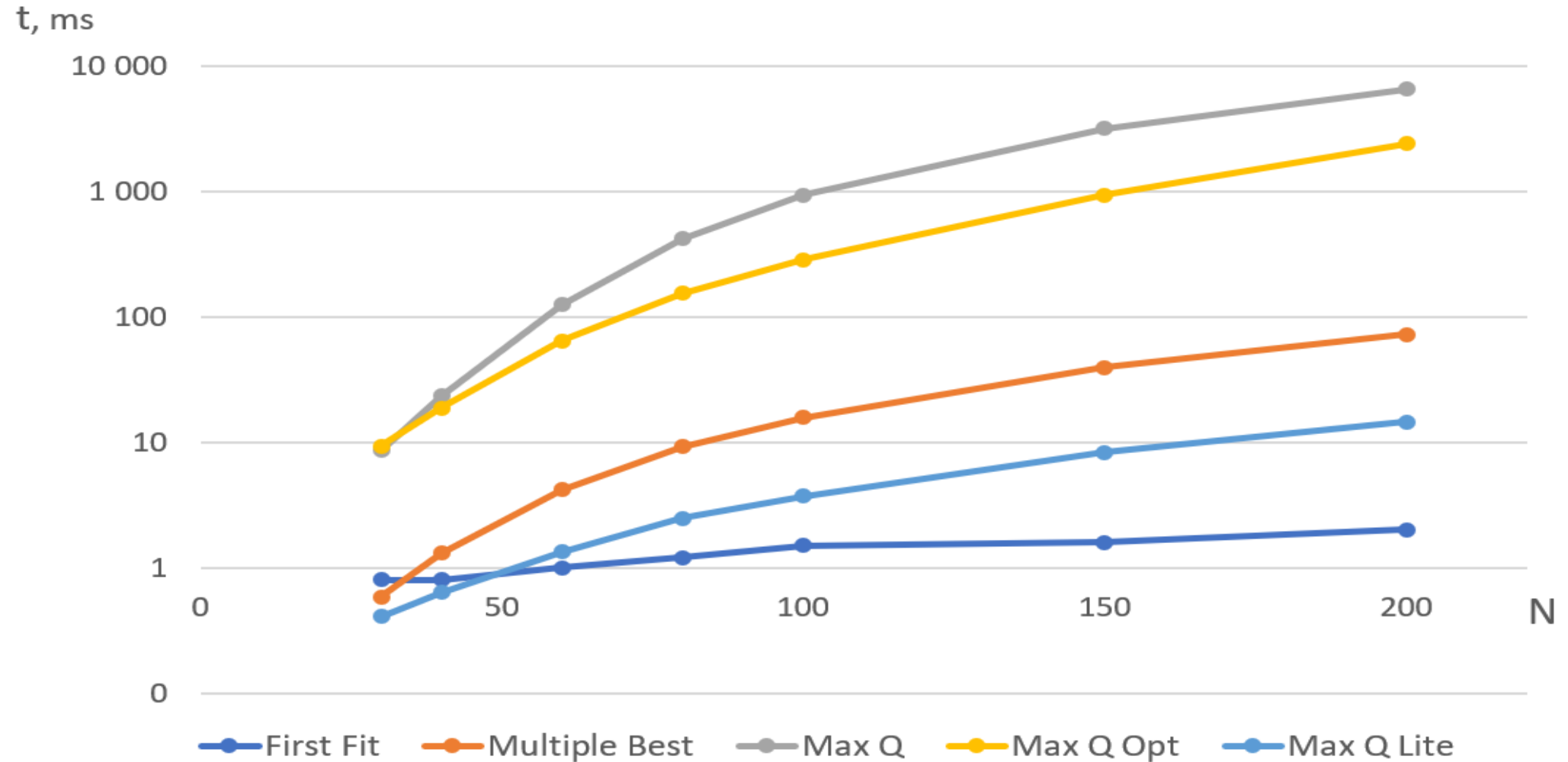
# Simulation Study: Custom Criterion

$Q = \text{sum of } q_i, i = 1, \dots, n, q_i \text{ in } [0;10], Q \text{ in } [0;70]$

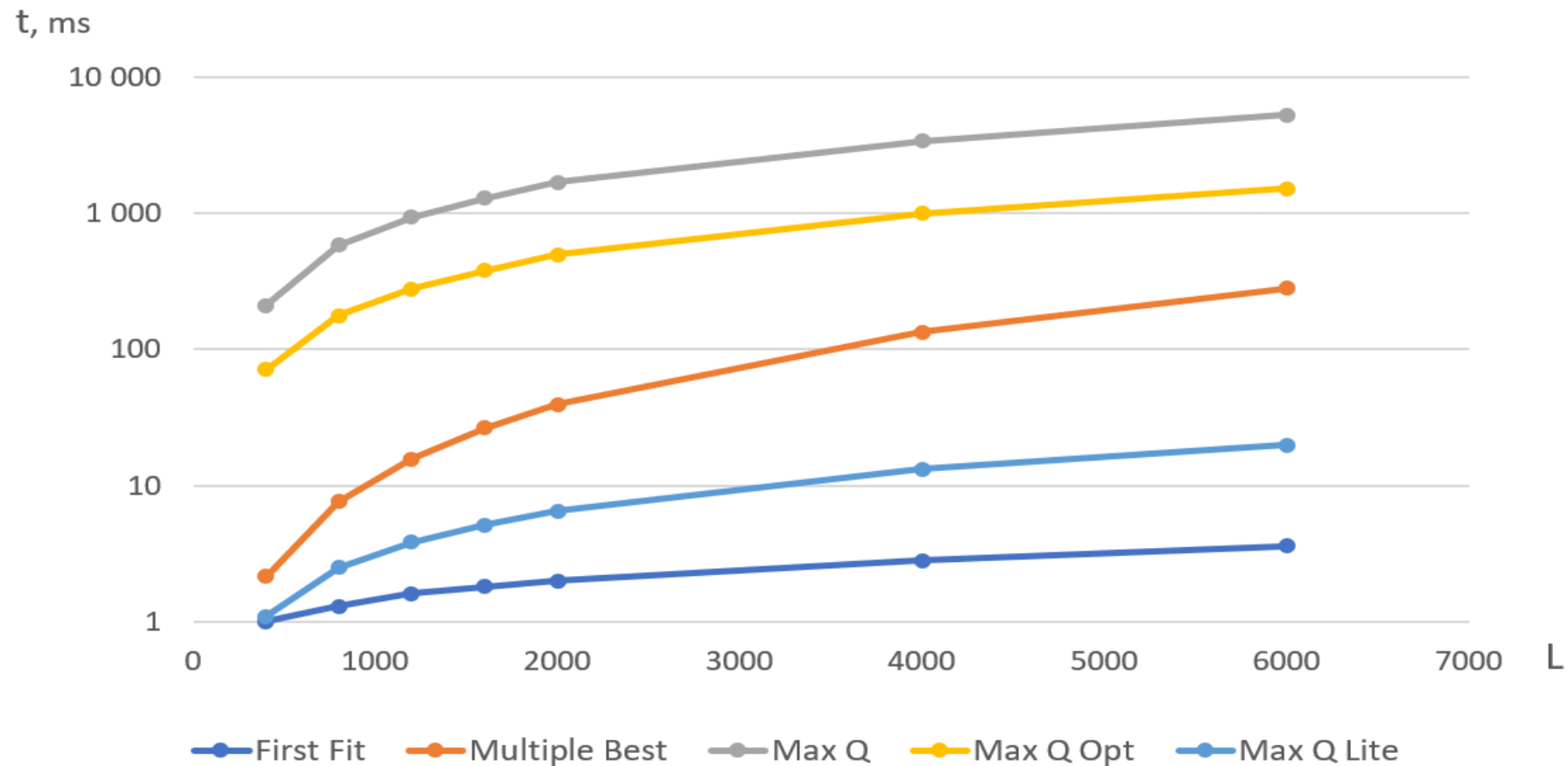


# Running Time and Complexity

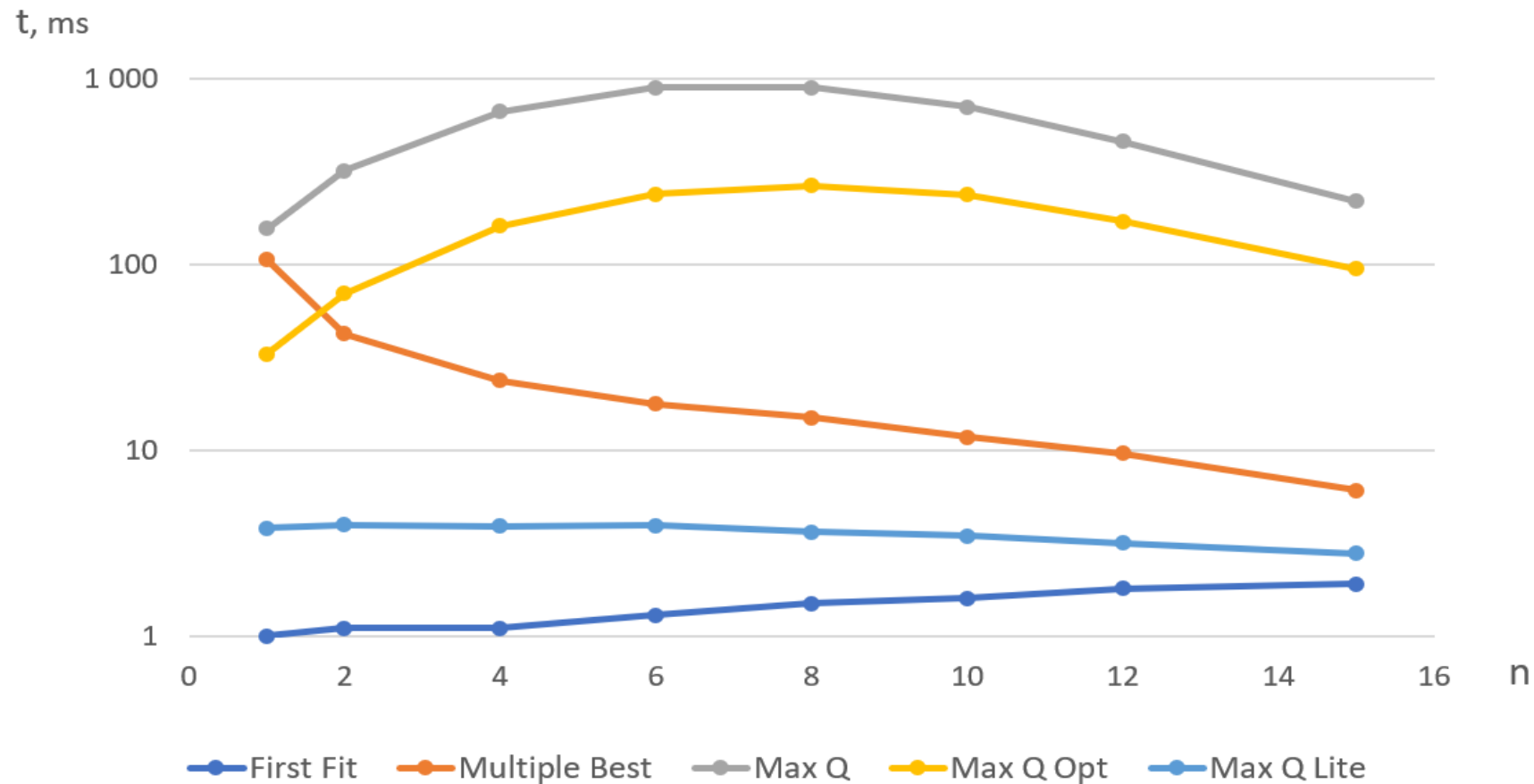
$$O(m * n * C)$$



# Running Time Depending on the Scheduling Interval Length $L$



# Running Time Depending on a Number $n$ of Nodes Required for a Job Execution



# Conclusions and Further Work

- The general square window search algorithm with the special slots subset allocation procedure is proposed for the resources co-allocation problem
- Simulation study proved 44% advantage over the First Fit algorithm and 18% over the MultipleBest optimization heuristic
- As a drawback, the general case algorithm requires 600 times longer realization time compared to FirstFit
- In our further work, we will be focused on a practical resources allocation tasks implementation based on the proposed general case approach

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# References

- <https://github.com/dmieter/mimapr>

CloudOfferFinder

SquareWindowFinder

- <https://srmpds.github.io/>

International Workshop on SRMPDS (Scheduling and Resource Management for Parallel and Distributed Systems) 2018, University of Oregon, USA

- <https://www.youtube.com/watch?v=h6KfBKdVHOU>

Victor Toporkov and Dmitry Yemelyanov. Resources Co-Allocation Optimization Algorithms for Distributed Computing Environments



Thank You!